

# Air Conditioning & Refrigeration

# Lectures

## Definitions and Moist Air Properties

## Definitions:

Air conditioning: Is the science and practice of controlling the indoor climate in term of temperature , air motion , humidity , air purity and noise.

Refrigeration: Is the process of removing the undesirable heat from a given body to maintain it at a desired lower temperature than its environment.

## Heating:

Is the transfer of heat to a space by virtue of a difference in temperature between the source and the space. This process may take by different forms such as direct radiation and free convection to the space.

## Cooling:

Is the transfer of heat from a space to a space by virtue of difference in temperature between the source and the space. In the usual cooling process air is circulated over a surface maintained at a low temperature.

## Humidification:

Is the transfer of water vapor to atmospheric air. Mass transfer is associated with heat transfer which causes an increase in the concentration of water vapor in the air.

## Dehumidification:

Is the transfer of water vapor from atmospheric air which lead to lower the concentration of water in the air. This process is mostly accomplished by circulating the air over a surface maintained at a sufficiently low temperature to cause the condensation of water vapor from the mixture.

## Cleaning:

The cleaning of air usually implies filtering the air to remove contaminant gases from air. Filtering is most often done by several types of filters.

## Air motion:

The motion of air in the vicinity of the occupant should be sufficiently gentle to create uniform comfort conditions in the space.

## Moist air :

Working substance in air conditioning is the moist air which is a mixture of two gases . One of these is dry air which itself is a mixture of a number of gases and the other is water vapor which may exist in a saturated or super heated state. Both are treated as perfect gases since both exist in the atmosphere at low pressures. In addition Gibbs–Dalton laws for non reactive mixture of gases can be applied to the dry air part only to obtain its properties as a single pure substance.

$$T_1 = T_2 = T$$

$$V_1 = V_2 = V$$

$$P_1 + P_2 = P$$

$$m_1 + m_2 = m$$

$$P_1 .V_1 = m_1 . R .T_1 \quad \& \quad P_2 .V_2 = m_2 .R.T_2$$

$$P_t = P_a + P_v$$

$$m_1.h_1 + m_2.h_2 = m.h$$

## Properties of moist air:

The properties of moist air are called psychrometric properties and the subject which deals with the behavior of moist air is known as psychrometry. In air conditioning practice all calculations on the dry air part since the water vapor part is continuously variable. The actual temperature of moist air is called the dry bulb temperature DBT . The total pressure which is equal to the barometric pressure is constant. The other relevant properties are :

Humidity ratio ( $\omega$ ), Relative Humidity ( $\phi$ ), Dew Point Temperature (DPT), Enthalpy ( $h$ ), Specific Heat ( $C_{p,h}$ ), and Wet Bulb Temperature (WBT).

## Humidity ratio or moisture content ( $\omega$ ):

$\omega = m.v/m_a = 0.622 * P_v/P_a = 0.622 * P_v/(P_t - P_v)$ , and  $P_v$  is:

$$P_v = P_s - P_{at} * A * (DBT - WBT)$$

Where A is constant =  $6.66 \text{ E-4 } 1/^\circ\text{C}$ , and

$P_{at}$  = atmospheric pressure.

## Relative humidity ( RH ):

$$RH = \phi \% = V_s/V_v = P_v/P_s$$

## Dew Point Temperature (DPT or $T_d$ ):

Is the temperature of saturated moist air at which the first drop of dew will be formed the moist air is cooled at constant pressure i.e. the water vapor in the mixture will start condensing.



## Enthalpy of moist air ( h ):

$h = h_a + \omega \cdot h_v$  where,  $h_a = C_{p,a} T = 1.005 T$  and,  
 $h_v = C_{p,w} T_d + h_{f,g} + C_{p,v} (T - T_d)$  at  $T_d = 0.0$ , Then:  
 $h_v = 2501 + C_{p,v} T = 2501 + 1.84 T$ , so that:  
 $h = 1.005 T + \omega ( 2501 + 1.84 T )$

## Humid specific heat (Cph ):

$$C_{p,h} = C_{p,a} + \omega * C_{p,v}$$

## Density of moist air (ρ):

It is the ratio of total mass of moist air to the volume:

$$\rho = (m_a + m_v) / V$$

## Wet bulb temperature ( WBT ):

Is the temperature of moist air reads by a wicked bulb thermometer with its wick is wetted by water.

## Latent heat ( $Q_L$ ) :

Is the heat added or removed from the moist air at constant DBT i.e. increases or decreases its moisture contents.

## Sensible heat ( $Q_s$ ):

Is the heat added or removed from the moist air at constant moisture content.

## Applications of air conditioning and refrigeration:

- Residential and industrial air conditioning.
- Air conditioning of vehicles.
- Food processing, storage and distribution.
- Chemical process in industries.
- Special applications of refrigeration.

## Examples:

1– Calculate the vapor pressure of moist air at a state of DBT = 20 °C , WBT = 15 °C and  $P_{a.t} = 95$  kPa.

Solution : from steam tables for  $P_{at} = 101.3$  kPa the saturation pressure is  $P_s = 1.704$  kPa at WBT = 15 °C.

Use the equation of vapor pressure :

$$P_v = P_s - P_{a.t} * A * (DBT - WBT)$$

$$P_v = 1.704 - 6.66 \text{ E-}4 * 95. * (20 - 15 ), \text{ then:}$$

$$P_v = 1.388 \text{ kPa.}$$

2- Calculate the relative humidity of moist air the state condition of example 1 .

Solution: at  $DBT = 20\text{ }^{\circ}\text{C}$  the saturated pressure  $P_s = 2.337\text{ kPa}$  therefore  $\phi \% = P_v/P_s = 1.388/2.337$   
 $\phi = 59.5\%$  .

3- Calculate the moisture content of moist air at the same state condition of example 1.

Solution:  $\omega = 0.622 ( P_v / P_a )$  and

$$P_a = P_{a.t} - P_v = 95. - 1.388$$

Then  $\omega = 0.00923\text{ kg water vapor / kg dry air.}$

4- Calculate the dew point of moist air at the same state condition of example 1.

Solution: The dew point temperature corresponding to  $P_v=1.388\text{ kPa}$  is about  $12\text{ }^{\circ}\text{C}$  from the steam table.

4- Calculate the specific volume of moist air at similar state of previous examples .

Solution : use the ideal gas law to the dry air alone .

$$V_a = m_a \cdot R_a \cdot T_a / P_a$$

$$P_a = P_{at} - P_v ; P_a = 95000 - 1388 = 93612 \text{ Pa}$$

$$\text{Then } V_a = 1 \cdot 287 \cdot (273 + 20) / 93612 = 0.898 \text{ m}^3$$

Consider water vapor mixed with the dry air.

$$V_v = m_v \cdot R_v \cdot T_v / P_v$$

$$V_v = 0.00923 \cdot 461 \cdot (273 + 20) / 1388 = 0.898 \text{ m}^3;$$

where for one kg of dry air  $\omega = m_v = 0.00923 \text{ kg}_{w.v} / \text{kg}_{d.a}$  It can be seen that the volume of dry air and that of water vapor are the same as explain earlier  $V = V_a = V_v$ .

5- Calculate the approximate enthalpy of humid air at DBT = 20 °C and WBT = 15 °C and 101.325 kPa .

$$h = 1.005 \cdot 20 + 0.00923 \cdot (2501 + 1.84 \cdot 20) = 43.5 \text{ kJ/kg}$$





## Psychrometric Chart:

All data essential for the complete thermodynamic and psychrometric analysis of air conditioning processes can be summarized in a psychrometric chart.

### PSYCHROMETRIC CHART

Based on a barometric pressure of 101.325 kPa

Sensible/total heat ratio for water added at 30°C

Specific enthalpy (kJ/kg)

Wet bulb temperature (°C) (sling)

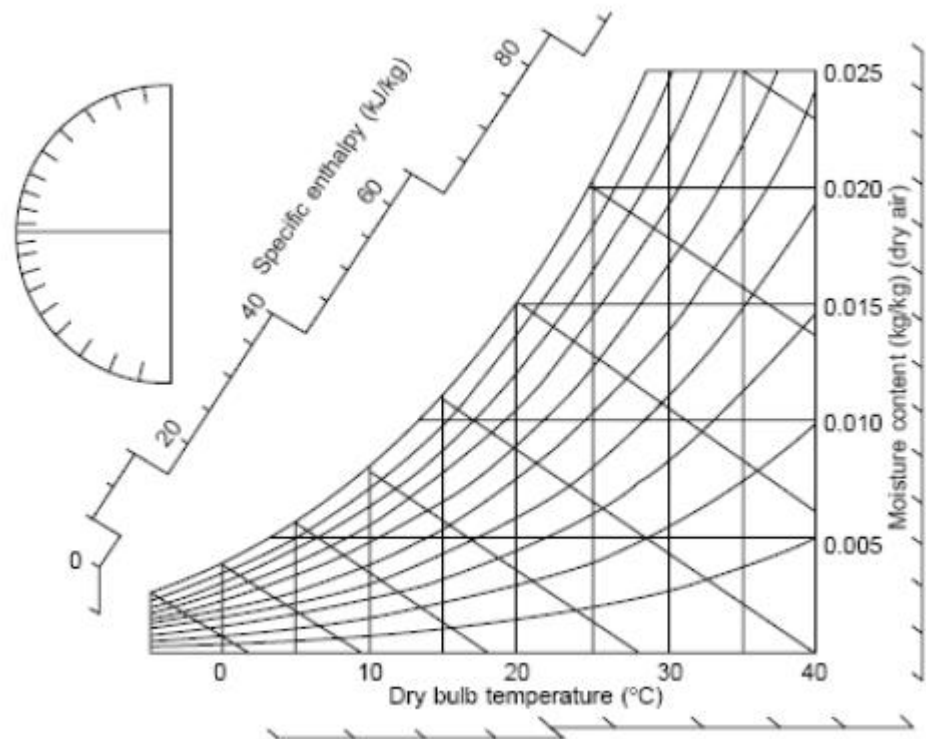
Specific volume (m<sup>3</sup>/kg)

Percentage saturation

Dry bulb temperature (°C)

Specific enthalpy (kJ/kg)

Moisture content (kg/kg) (dry air)



The chart which is most commonly used is  $\omega$  vs. DBT. The chart is normally constructed for a standard atmospheric pressure of 101.325 kPa corresponding to the pressure at the mean sea level. The saturation line on the chart is the line of 100% RH and for all points on this line  $P_v = P_s$ .

Similarly one can show the lines of constant thermodynamic Wet bulb temperature, constant specific enthalpy and constant specific volume. The particular psychrometric chart given in the figure is for normal DBT range of 0 °C to 50 °C and humidity ratios of 0.0 to 0.03 kg/kg dry air. Psychrometric charts for other conditions such as subzero or high temperature can also be prepared.



## Properties of Air

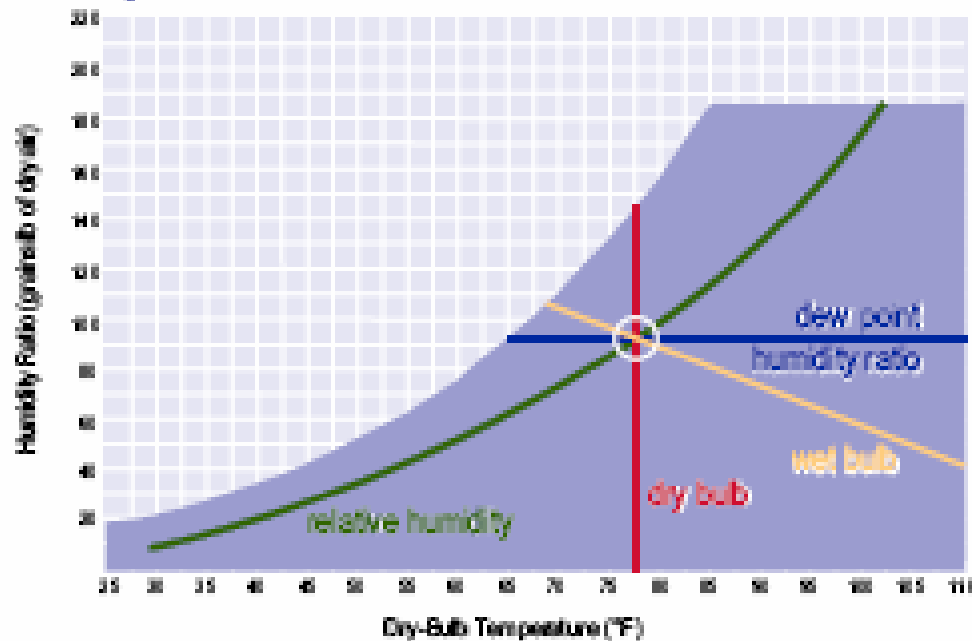


Figure 83

The lines of the psychrometric chart represent five physical properties of air: **dry bulb**, **wet bulb**, **dew point**, **humidity ratio**, and **relative humidity**. If any two of these properties are known, the remaining properties can be determined from the chart.

## Examples :

1– A sample of moist air has a DBT of  $43\text{ }^{\circ}\text{C}$  and WBT of  $29\text{ }^{\circ}\text{C}$  , find using the psych. chart the following :

- a– Specific humidity
- b– Relative humidity
- c– Dew point temperature
- d– Specific enthalpy
- e– Specific volume.

2– A sample of moist air has DBT of  $24\text{ }^{\circ}\text{C}$  and at a saturation state , find using Psych. chart :

- a– Specific humidity
- b– Relative humidity
- c– Dew point temperature
- d– Specific enthalpy
- e– Specific volume.

3– A sample of moist air has DBT of 30 °C and with dry state , find the following using psych. chart .

- a– Specific humidity
- b– Relative humidity
- c– Dew point temperature
- d– Specific enthalpy
- e– Specific volume.

4– A sample of moist air has a DBT of 35 °C and WBT of 15 °C at  $P_a=101.325$  kPa, find using psych. chart the following:

- a– Specific humidity
- b– Relative humidity
- c– Dew point temperature
- d– Specific enthalpy
- e– Specific volume.

**Thank You**



# Air Conditioning & Refrigeration

# Lectures

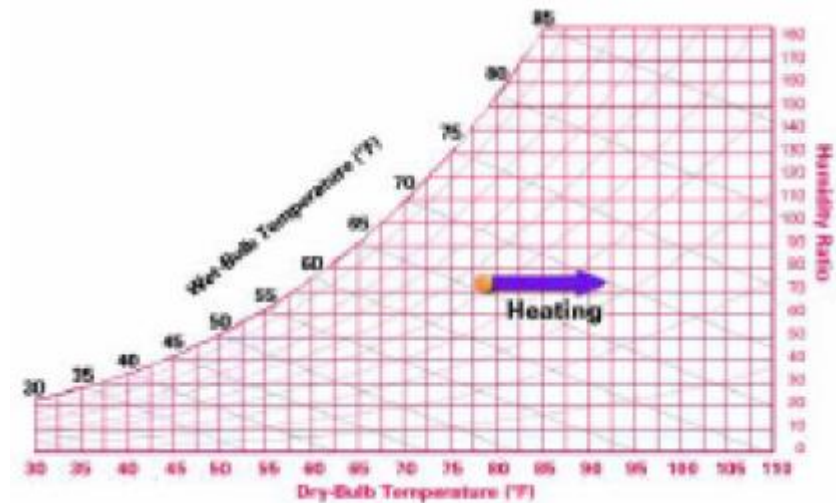
## Air Conditioning Processes

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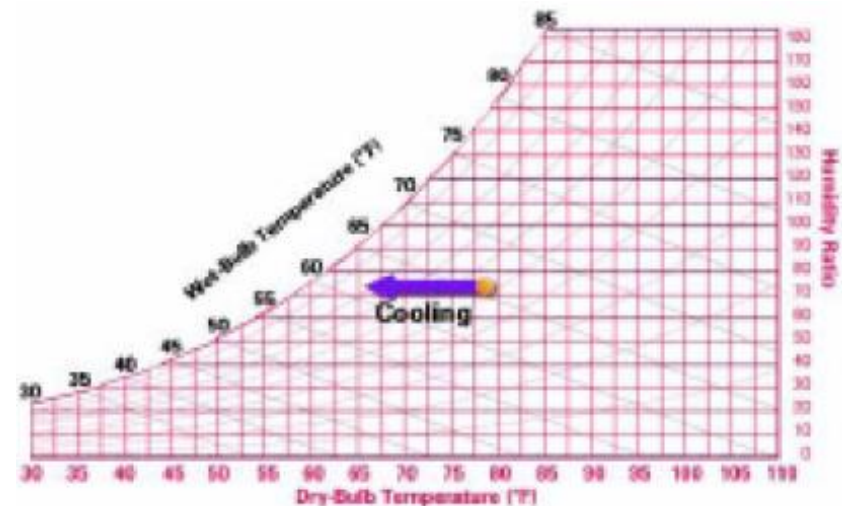
- **Sensible Heating**

If sensible heat is added to air, the air condition moves horizontally to the right.



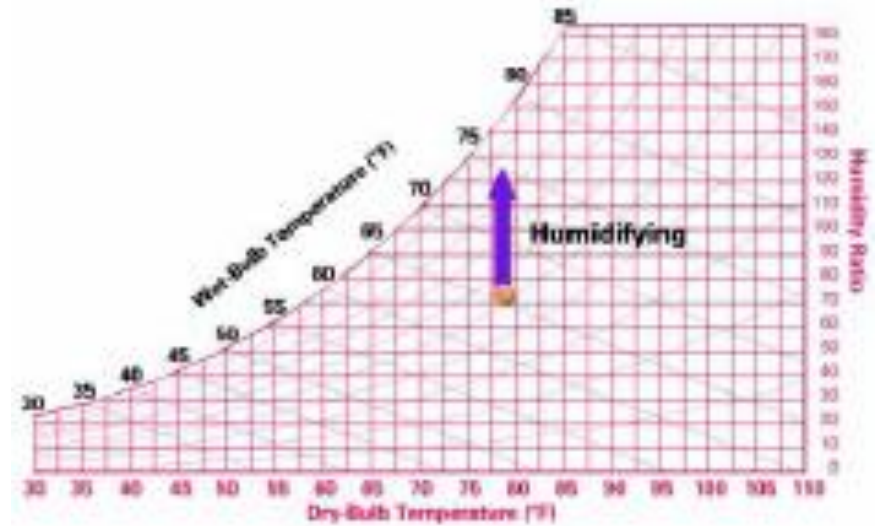
- **Sensible Cooling**

If sensible heat is removed from air, the air condition moves horizontally to the left.



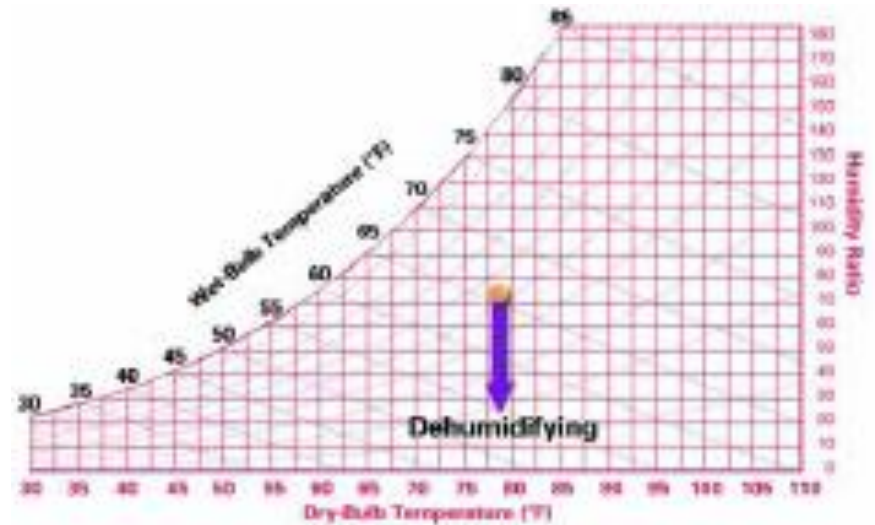
- **Humidification**

If moisture is added to air without changing the dry bulb temperature, the air condition moves upward along the dry bulb temperature line.



- **Dehumidification**

If moisture is removed from Air without changing the dry bulb temperature, the air condition moves downward along the dry bulb temperature line.





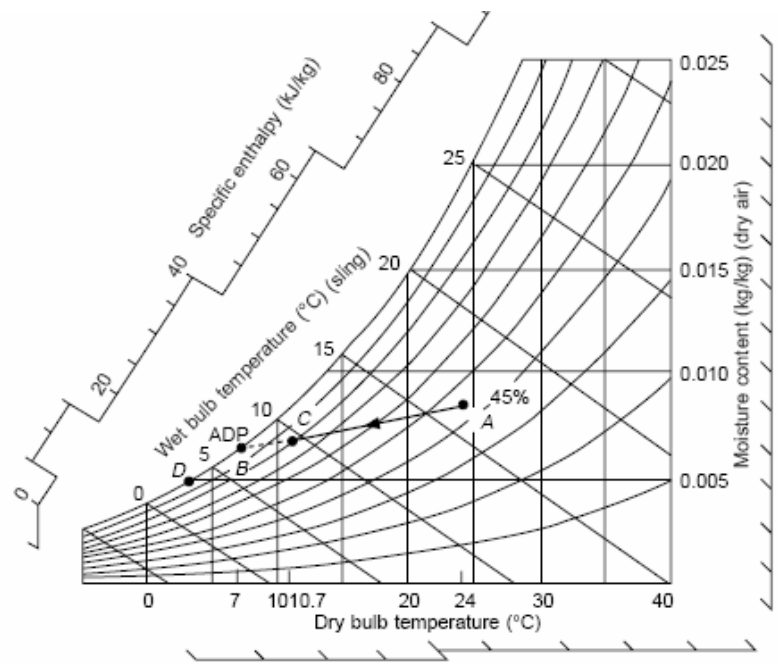
There are several methods that may be used to carry out the dehumidification process:

- i) cooling the air to temperature below its dew point,
- ii) using absorption process,
- iii) using adsorption materials,
- iv) compress and cool the air.

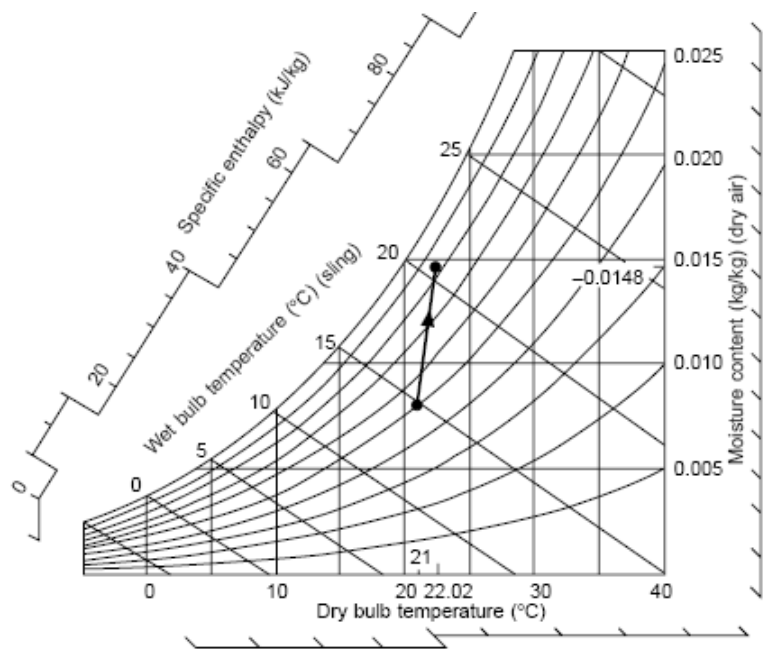
The first method represents the normal practice to cool and dehumidify the moist air in air conditioning systems.

Humidification of air can take place by injecting saturated or super heated steams inside the air conditioning ducts using fine nozzles and the equipment is called a humidifier.

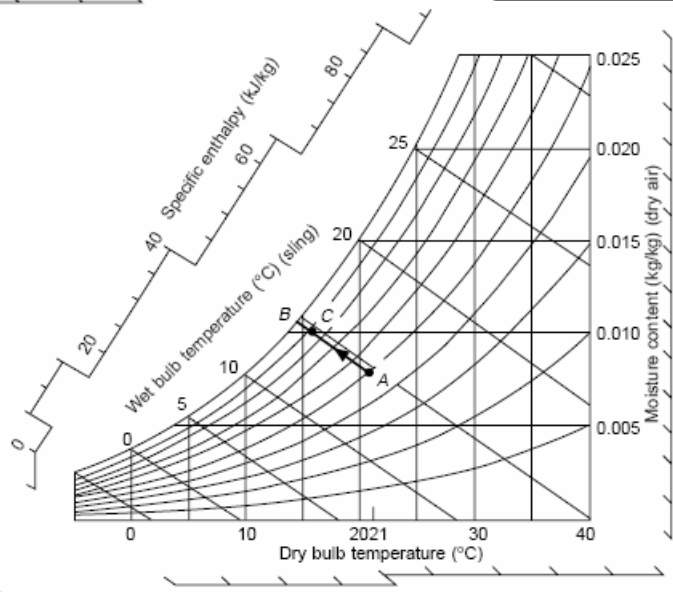
# Cooling & Dehumidification



# Heating & Humidification



# Adiabatic Cooling



## Examples :

1– Air at a state of DBT = 14 °C, RH=50% is passed through a heating coil. The DBT is increased upto 42 °C. Moisture content remain constant in this process, find :

- a) WBT of the exit air.
- b) The dew point temperature.
- c) The sensible heat added by HC for 1.0 kg/s of air.

Answers : a) 19.5°C , b) 3.9°C , c) 28.6 kW

2–Air at condition of DBT = 45°C , RH= 20 % enter to an air cooler and exit at RH= 60 % , find :

- a) DBT of exit air.
- b) The moisture content ( $\omega$ ) at exit.
- c) Plot the psychrometric process.

Answers: a) 31.5 °C, b) 17.5 gwv /kg da .

3- Moist air at DBT = 30°C and WBT = 25°C enter a cooling coil and exit from it at saturation state with DBT = 15 °C. IF the air is supplied to the coil at 3 m<sup>3</sup>/s, find:

- All the properties of air at inlet and outlet.
- The sensible heat removed by the cooling coil.
- Amount of moisture removed from the air by CC.

Answers:

- a)  $h_{in} = 76 \text{ kJ/kg}$  ,  $\omega_1 = 0.010 \text{ kg}_{w.v}/\text{kg}_{d.a.}$  ,  $v_1 = 0.882 \text{ m}^3/\text{s}$  ,  
 $RH_1 = 66$  ,  $T_{d.p} = 23.2 \text{ }^\circ\text{C}$  ,  $h_2 = 42 \text{ kJ/kg}$  ,  $\omega_2 = 0.0107$   
 $\text{kg}_{w.v}/\text{kg}_{d.a.}$  ,  $v_2 = 0.831 \text{ m}^3/\text{kg}$  ,  $RH_2 = 100 \%$
- b) 115.6 kW, c) 0.0248 kg<sub>wv</sub>/kg<sub>da</sub>.

**Thank You**



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## Air Conditioning Processes

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## Mixing process:

Adiabatic mixing of different quantities of air in two different states at constant pressure. The conditions of the mixing state may be found by the following relations and as shown the figure below :

$$T_3 = (m_1 \cdot T_1 + m_2 \cdot T_2) / (m_1 + m_2) \text{ or;}$$

$$h_3 = (m_1 \cdot h_1 + m_2 \cdot h_2) / (m_1 + m_2) \text{ or;}$$

$$\omega_3 = (m_1 \cdot \omega_1 + m_2 \cdot \omega_2) / (m_1 + m_2) ; \text{where } m \text{ in kg/s}$$

It is acceptable practice in air conditioning to use volume ratio rather than mass ratio:

$$T_3 = (v_1 \cdot T_1 + v_2 \cdot T_2) / (v_1 + v_2) ;$$

$$h_3 = (v_1 \cdot h_1 + v_2 \cdot h_2) / (v_1 + v_2) ; \text{ and for } \omega$$

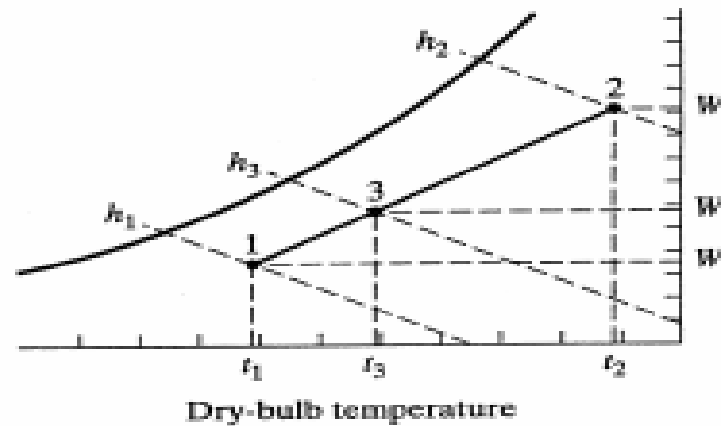
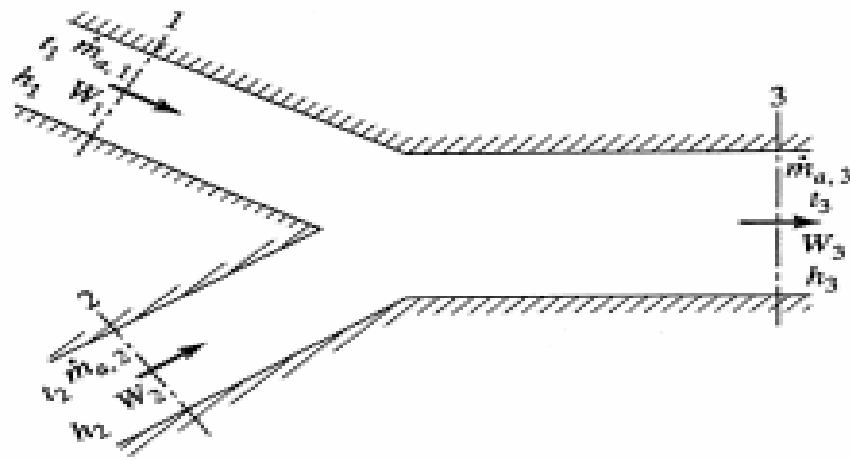
$$\omega_3 = (v_1 \cdot \omega_1 + v_2 \cdot \omega_2) / (v_1 + v_2) ; \text{where } v \text{ in m}^3/\text{s}$$



## Example :

An air stream at  $DBT=21^{\circ}\text{C}$  ,  $WBT=14^{\circ}\text{C}$  is mixed with an other one at  $DBT=28^{\circ}\text{C}$  ,  $WBT=20^{\circ}\text{C}$ . The mass flow rates were  $1\text{ kg/s}$  for the first and  $3\text{ kg/s}$  for the second. Find the moisture content, enthalpy, and the DBT for the mixture and plot the process on the chart.

Answers :  $0.01\text{ kg}_{w.v}/\text{kg}_{d.a}$  ,  $52.15\text{ kJ/kg}$  ,  $26.25^{\circ}\text{C}$ .



## Air Conditioning Cycles :

There are two air conditioning cycle one for summer air conditioning and the other for winter air conditioning.

The summer cycle has three types:

- i) All out side air,
- ii) All return air, and,
- iii) Mixed air.

The winter air conditioning cycle can be done into two methods:

- i) The first method is to preheat the air and then cooling it adiabatically up to a given point and then reheat it to the supply conditions.
- ii) The second method is to use an air washer to humidify the air up to a given point then reheat it to the supply conditions.

# Psychrometric analysis

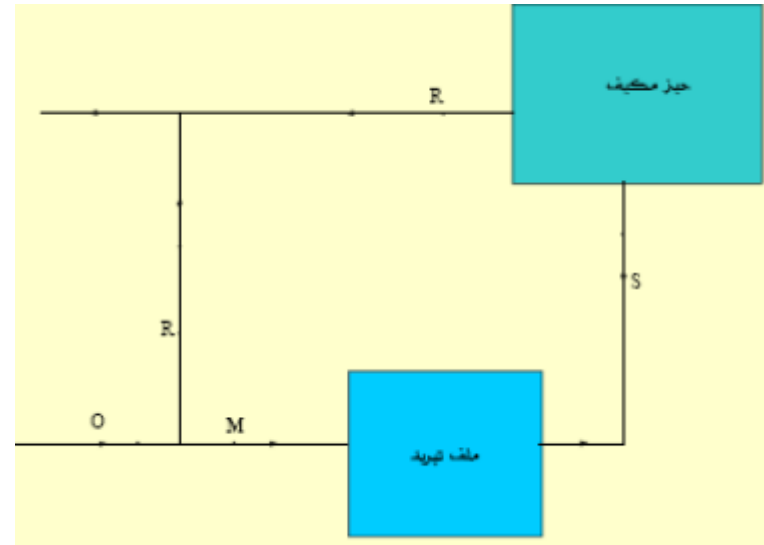
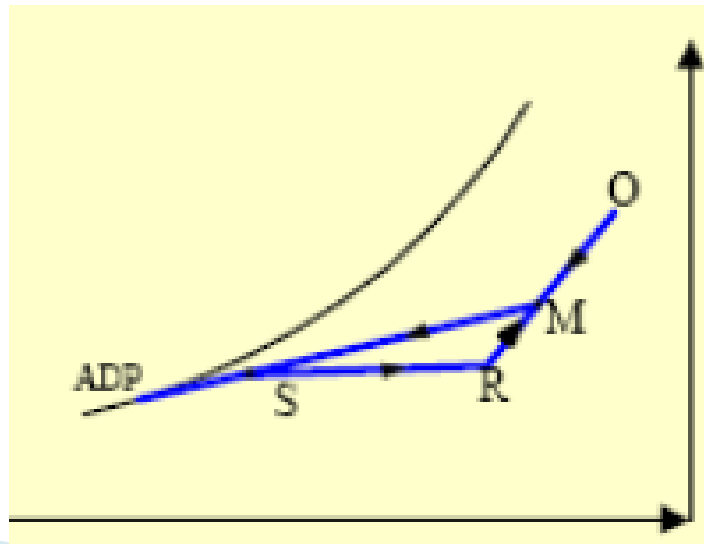
These analysis include summer air conditioning cycles and winter air conditioning cycles.

Summer cooling and dehumidification processes:

1- All outside air,

2- All return air,

3- Mixing of fresh air with return air as shown below.



## Calculation procedure for mixing cycle :

The following steps is required to carry the analysis:

- Mark the inside and out side conditions on the chart .
- Calculate the  $SHF=Q_s/(Q_s + Q_l)$  { if the sensible and latent heat are given}, and plot it as a parallel line starting from the inside conditions.
- Plot the supply condition. IF other conditions are given also plot them.
- Calculate the mixing conditions and plot them on the line between the inside and out side conditions.
- Connect the mixing point with the supply point by a line and find  $T_{a.d.p}$  which represent the point where this line cross the saturation line.
- Calculate BPF and other required quantities.  
Where  $BPF=(T_s-T_{a.d.p})/(T_m-T_{a.d.p})$

Use the following equations to calculate the required variables:

$$Q_{s,r} = 1.22 * V_s * (T_r - T_s) , \text{ this can be used to find } V_s.$$

$$Q_{\text{coil}} = 1.2 * V_s * (h_m - h_s) , \text{ for mixed air,}$$

$$Q_{\text{coil}} = 1.2 * V_s * (h_o - h_s) , \text{ for all outside air,}$$

$$Q_{\text{coil}} = 1.2 * V_s * (h_r - h_s) , \text{ for all return air,}$$

$$m_{\text{vap}} = m_s * \Delta\omega , \text{ and the three conditions as in } Q_{\text{coil}},$$

$$Q_{\text{chilled water}} = m_{\text{water}} * c_{\text{pw}} * \Delta T_{\text{water}}, \text{ Where } c_{\text{pw}} = 4.2 \text{ kJ/kgK}$$

## Examples:

1 – An air conditioned space is maintained at DBT=24°C and RH=50% .The out side condition is DBT=38 °C with WBT=27°C.The space has a sensible heat gain of 24 kW and latent heat of 6kW. Use all out side air system find:

- i) the supply condition of the air if the relative humidity at the supply point is taken to be 90%.
- ii) volume flow rate of supplied air.
- iii) the total cooling load of the cooling coil.
- iv) the chilled water volume flow rate if its temperature rise is 5.6°C.

Answers :  $T_s=12.2$  °C,  $h_s=32.6$  kJ/kg,  $Q_{coil}=95.6$  kW,  $1.06$  m<sup>3</sup>/s .

2– The sensible heat gain of a given space is 50 kW and its latent load is 15 kW. The inside condition is 26 °C with 50% relative humidity. The space is air conditioned using all return air system. Find by assuming 90% saturation for the supply air:

i) the supply conditioned of the air, ii) volume flow rate of supplied air, iii) cooling coil load.

Answers :  $T_s = 14.5^\circ\text{C}$ ,  $h_s = 38.2 \text{ kJ/kg}$ ,  $v_s = 3.56 \text{ m}^3/\text{s}$ ,  $Q_{\text{coil}} = 65 \text{ kW}$ .

3– An air conditioned space with inside condition of  $\text{DBT} = 25.5^\circ\text{C}$ ,  $\text{WBT} = 18^\circ\text{C}$  has a sensible heat = 17.5 kW and a latent heat = 12.3 kW. The space required an outside air of  $0.35 \text{ m}^3/\text{s}$  at  $\text{DBT} = 32.5^\circ\text{C}$ ,  $\text{RH} = 50\%$ . If  $\text{RH}_s = 90\%$ , find: i) state of the supplied air and its mass flow rate, ii) cooling coil load, Plot the process on chart and calculate the BPF.

Answers:  $T_s = 11.5^\circ\text{C}$ ,  $h_s = 29.5 \text{ kJ/kg}$ ,  $m_s = 0.813 \text{ kg/s}$ ,  $Q_{\text{coil}} = 24.8 \text{ kW}$ ,  $\text{BPF} = 0.25$

4- An air conditioned space is need to be maintained at DBT=24 °C, RH= 50%. The space required 28.3 m<sup>3</sup>/min fresh air. The sensible heat loss of the space is 66 kW and its latent is 16.5 kW. The outside design condition is DBT=7 °C, RH= 80% . The mixed air is passes through a steam humidifier followed by a heating coil. The humidifier efficiency is 85% and the coil is heated the air up to 49 °C, plot the air conditioning process on the chart, and find:

- i) The supplied air mass flow rate at a given  $T_s = 49$  °C,
- ii) the heating coil load.
- iii) the humidifier heating load,
- iv) the amount of steam required by the humidifier.

Answers:  $m_s = 2.77$  kg/s,  $Q_{coil} = 78.0$  kW,  $Q_{hum} = 16.9$  kW ,  $m_{vap} = 0.00825$  kg/s



**Thank You**

